Name: $\qquad$
Instructor: $\qquad$

## Math 10550, Exam II

October 17, 2013

- The Honor Code is in effect for this examination. All work is to be your own.
- No calculators.
- The exam lasts for 1 hr . and 15 m ..
- Be sure that your name is on every page in case pages become detached.
- Be sure that you have all 10 pages of the test.

| PLEASE MARK YOUR ANSWERS WITH AN X, not a circle! |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1. (a) | (b) | (c) | (d) | (e) |
| 2. (a) | (b) | (c) | (d) | (e) |
| 3. (a) | (b) | (c) | (d) | (e) |
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| 10. (a) | (b) | (c) | (d) | (e) |


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| Multiple Choice__ |
| 11. |
| 12. |
| 13. |
| Total |

Name: $\qquad$
Instructor: $\qquad$

## Multiple Choice

1. ( 6 pts.) A particle is moving along an axis. Its position at time $t$ (seconds) is given by

$$
s(t)=t^{3}-6 t^{2}+9 t
$$

where $s(t)$ is measured in feet. What is the total distance travelled by the particle between $t=0$ and $t=2$ seconds.
(a) 6 feet
(b) 10 feet
(c) 2 feet
(d) 4 feet
(e) 5 feet
2.( 6 pts .) The height of a rectangle is increasing at a rate of $8 \mathrm{~cm} / \mathrm{s}$ and its width is increasing at a rate of $3 \mathrm{~cm} / \mathrm{s}$. When the height is 20 cm and the width is 10 cm , how fast is the area of the rectangle increasing?
(a) $190 \mathrm{~cm}^{2} / \mathrm{s}$
(b) $211 \mathrm{~cm}^{2} / \mathrm{s}$
(c) $140 \mathrm{~cm}^{2} / \mathrm{s}$
(d) $11 \mathrm{~cm}^{2} / \mathrm{s}$
(e) $24 \mathrm{~cm}^{2} / \mathrm{s}$

Name: $\qquad$
Instructor: $\qquad$
3. $\left(6 \mathrm{pts}\right.$.) Use linear approximation of $f(x)=\frac{1}{\sqrt{x}}$ at $a=4$ to estimate $\frac{1}{\sqrt{3.9}}$.
(a) $\frac{1}{\sqrt{3.9}} \approx \frac{79}{160}$
(b) $\frac{1}{\sqrt{3.9}} \approx \frac{11}{20}$
(c) $\frac{1}{\sqrt{3.9}} \approx \frac{1}{2}$
(d) $\frac{1}{\sqrt{3.9}} \approx \frac{9}{20}$
(e) $\frac{1}{\sqrt{3.9}} \approx \frac{81}{160}$
4. (6 pts.) Find the linearization $L(x)$ of the function $f(x)=\sin (2 x)$ at $a=\frac{\pi}{4}$.
(a) $\quad L(x)=1-\frac{\sqrt{2} \pi}{4}+\sqrt{2} x(\mathrm{~b}) \quad L(x)=1$
(c) $\quad L(x)=1-\frac{\pi}{2}+2 x$
(d) $L(x)=1+x$
(e) $\quad L(x)=1+\frac{\pi}{2}-2 x$

Name:
Instructor: $\qquad$
5. ( 6 pts.) Find all critical points (critical numbers) of

$$
f(x)=x^{4}+\frac{16}{3} x^{3}-10 x^{2}-12
$$

(a) $x=-2,0,2$
(b) $\quad x=5,0,-1$
(c) $x=-5,1$
(d) $\quad x=0,-2$
(e) $x=-5,0,1$
6. (6 pts.) Let

$$
f(x)=x^{3}+3 x^{2}-24 x .
$$

Find the absolute maximum and absolute minimum values of $f$ on the interval $[0,10]$.
(a) Max at $x=4$; Min at $x=0$.
(b) Max at $x=10$; Min at $x=0$.
(c) Max at $x=4$; Min at $x=1$.
(d) Max at $x=10$; Min at $x=2$.
(e) Max at $x=8$; Min at $x=2$.

Name: $\qquad$
Instructor: $\qquad$
7. ( 6 pts.) Find the local maxima and minima of

$$
f(x)=3 x^{2 / 3}-x
$$

where $f(x)$ is defined for all real numbers $x$.
(a) $\quad f$ has a local minimum at $x=0$ and a local maximum at $x=8$.
(b) $\quad f$ has a local maximum at $x=8$ and no local minimum.
(c) $\quad f$ has a local maximum at $x=0$ and a local minimum at $x=1 / 8$.
(d) $\quad f$ has a local minimum at $x=0$ and a local maximum at $x=1 / 8$.
(e) $f$ has a local maximum at $x=1 / 8$ and no local minimum.
8. (6 pts.) Let

$$
f(x)=\frac{1}{3} x^{3}-\frac{3}{2} x^{2}+2 x+10
$$

On which of the following intervals is the graph of the function $f$ both decreasing and concave upward on the entire interval?
(a) $(-\infty, 2)$
(b) $(1,2)$
(c) $\left(-\infty, \frac{3}{2}\right)$
(d) $\left(\frac{3}{2}, 2\right)$
(e) $(0,2)$

Name:
Instructor: $\qquad$
9. ( 6 pts .) Consider the function

$$
f(x)=\frac{3 x^{3}-3}{(2 x+2)\left(x^{2}-7 x+10\right)}
$$

Which of the following is true?
(a) $\quad f$ has a horizontal asymptote at $y=1$ and vertical asymptotes at $x=-1,2,5$.
(b) $\quad f$ has a horizontal asymptote at $y=\frac{3}{2}$ and vertical asymptotes at $x=1,2,5$.
(c) $\quad f$ has a horizontal asymptote at $y=\frac{3}{2}$ and vertical asymptotes at $x=-1,2,5$.
(d) $\quad f$ has a horizontal asymptote at $y=-1$ and vertical asymptotes at $x=-1,2,5$.
(e) $f$ has a horizontal asymptote at $y=\frac{3}{2},-\frac{3}{2}$ and vertical asymptotes at $x=-1,2,5$.

Name: $\qquad$
Instructor: $\qquad$
10. ( 6 pts.) Let $f$ be a function of $x$. The table below shows whether the functions $f^{\prime}(x)$ and $f^{\prime \prime}(x)$ are positive, negative or have value 0 at each of the given values of $x$.

| $x$ | -2 | 0 | 2 |
| :---: | :---: | :---: | :---: |
| $f^{\prime}(x)$ | $=0$ | $=0$ | $=0$ |
| $f^{\prime \prime}(x)$ | $>0$ | $=0$ | $<0$ |

Which of the graphs shown below is a feasible graph of $f(x)$ ?
(Note that the label for each graph is given on the lower left of the graph.)
(a)

(b)

(c)

(d)

(e) None of the above

Name:
Instructor:

## Partial Credit

You must show your work on the partial credit problems to receive credit!
11.(13 pts.) Show that

$$
x^{5}+2 x^{3}+2 x-3=0
$$

has one and exactly one solution. Identify the theorem(s) you are using.

Name: $\qquad$
Instructor: $\qquad$
12.(13 pts.) Car $A$ and car $B$ are approaching the intersection " $C$ " of two streets intersecting at a right angle. Car $A$ is going South at 45 mph , car $B$ is heading West at 30 mph . We denote the angle $\angle(C, B, A)$ by $\theta$ (measured in radians), the distance from $C$ to $B$ by $x$, and the distance from $C$ to $A$ by $y$. At what rate is the angle $\theta$ changing when car $A$ and car $B$ are both 1 mile from the intersection?


Name: $\qquad$
Instructor: $\qquad$
13. (14 pts.) Suppose $f(x)$ is a function which is continuous and differentiable on the interval $\left(-\frac{3 \pi}{4}, \frac{3 \pi}{4}\right)$ with

$$
f^{\prime}(x)=1-\sin ^{2} x
$$

Warning: the formula shown above is for the DERIVATIVE of $f(x)$
(a) Find all critical points (critical numbers) of the function $f(x)$ in the given interval.
(b) List the subintervals of $\left(-\frac{3 \pi}{4}, \frac{3 \pi}{4}\right)$ where $f$ is increasing / decreasing.
(c) List all local maxima and local minima of $f$ in the interval $\left(-\frac{3 \pi}{4}, \frac{3 \pi}{4}\right)$, or say so if there are none.
(d) List the subintervals of $\left(-\frac{3 \pi}{4}, \frac{3 \pi}{4}\right)$ where $f$ is concave up / concave down.
(e) List all inflection points of $f$ in the interval $\left(-\frac{3 \pi}{4}, \frac{3 \pi}{4}\right)$, or say so if there are none.

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